

Chapter 9 / Example 11

Initial state vectors

Dockless bicycle company Mathbike open their business by distributing a number of bicycles in a city according to the initial state vector $S_0 = \begin{pmatrix} 110 \\ 80 \\ 50 \end{pmatrix}$.

- Calculate the likely number of bicycles in each zone of the city after 5 days using the transition matrix given in example 10.
- Find the likely steady state of Mathbikes.

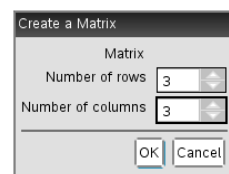
Enter the transition matrix $T = \begin{pmatrix} 0.50 & 0.30 & 0.10 \\ 0.30 & 0.35 & 0.30 \\ 0.20 & 0.35 & 0.60 \end{pmatrix}$.

Open a new document and add a Calculator page.

Press **menu** 7:Matrix & Vector | 1:Create | 1:Matrix.

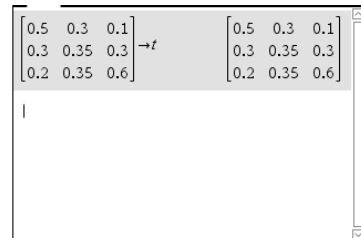
Change the number of rows and columns to 3.

Press **enter**.



Enter the values of the elements of the matrix T , using **tab** to move through the matrix.

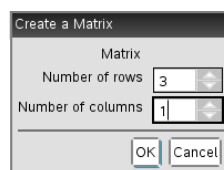
Press **ctrl** **var** **sto→** T and press **enter**.



Press **menu** 7:Matrix & Vector | 1:Create | 1:Matrix.

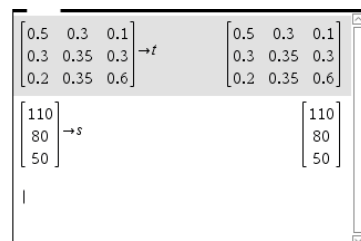
Change the number of rows to 3 and columns to 1.

Press **enter**.



Enter the values of the elements of the matrix S , using **tab** to move through the matrix.

Press **ctrl** **var** **sto→** S and press **enter**.



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Initial state vectors

Type $t^5 \times s$ and press **enter**.

There would be approximately 66 Mathbikes in zone C, 76 in Zone I and 98 in Zone O.

$\begin{bmatrix} 0.2 & 0.35 & 0.6 \end{bmatrix}$	$\begin{bmatrix} 110 \\ 80 \\ 50 \end{bmatrix} \rightarrow s$	$\begin{bmatrix} 110 \\ 80 \\ 50 \end{bmatrix}$
$t^5 \cdot s$		$\begin{bmatrix} 65.7459 \\ 75.7895 \\ 98.4646 \end{bmatrix}$

Repeat the calculation with some higher powers of the matrix.

The system reaches an equilibrium at 65 bikes in C, 76 in I and 99 in O.

$\begin{bmatrix} 0.2 & 0.35 & 0.6 \end{bmatrix}$	$\begin{bmatrix} 50 \\ 50 \\ 50 \end{bmatrix} \rightarrow s$	$\begin{bmatrix} 50 \\ 50 \\ 50 \end{bmatrix}$
$t^5 \cdot s$		$\begin{bmatrix} 65.7459 \\ 75.7895 \\ 98.4646 \end{bmatrix}$
$t^{500} \cdot s$		$\begin{bmatrix} 65.2632 \\ 75.7895 \\ 98.9474 \end{bmatrix}$